

11 The functions  $f$  and  $g$  are defined by

$$f(x) = \frac{2}{x+1}, x > 0 \quad g(x) = 1 - x^2, x \in \mathbb{R}.$$

- a Find  $fg(x)$ , giving your answer in its simplest form.
- b Find  $f^{-1}(x)$ .
- c Solve the equation  $f(x) = f^{-1}(x)$ .

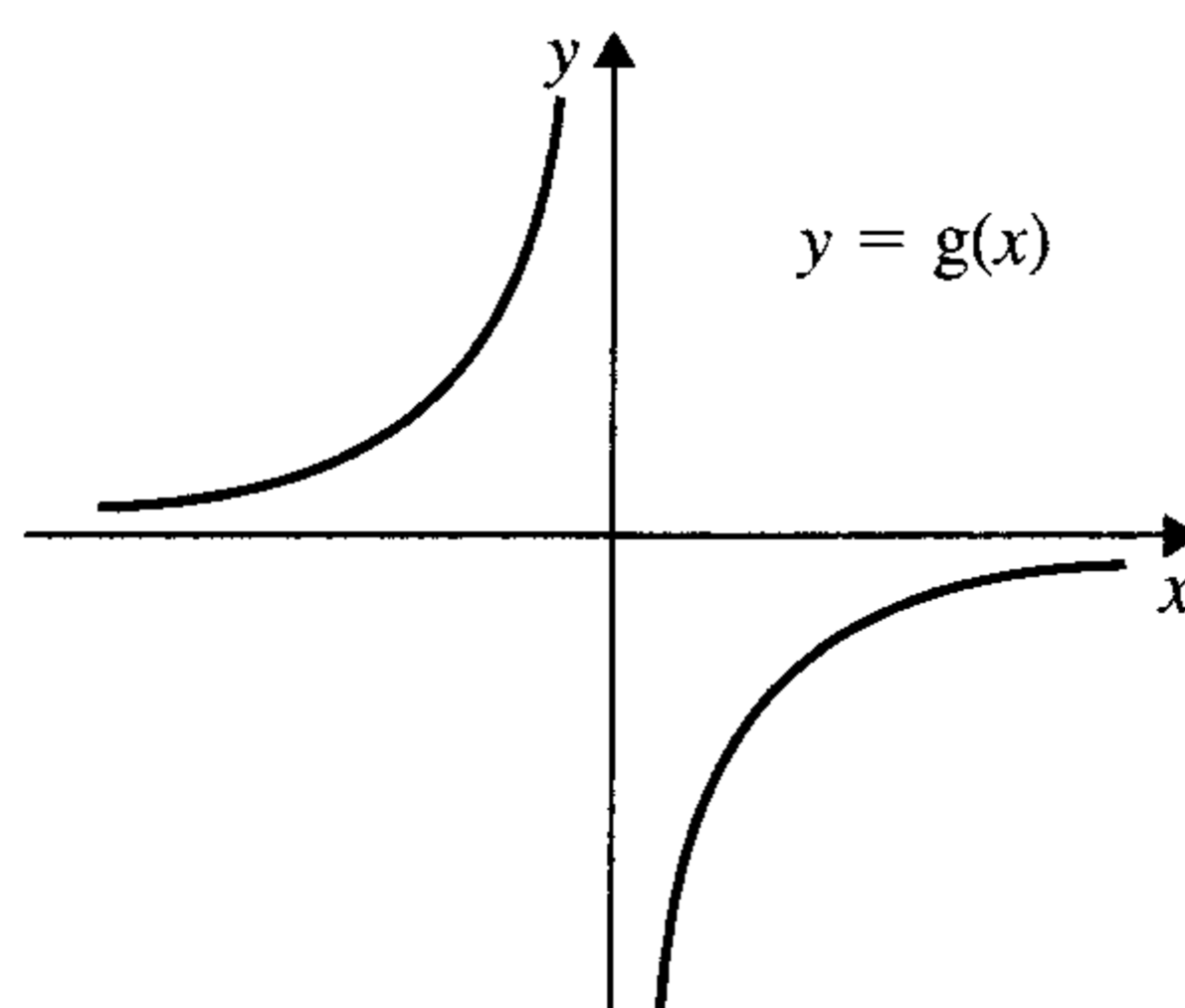
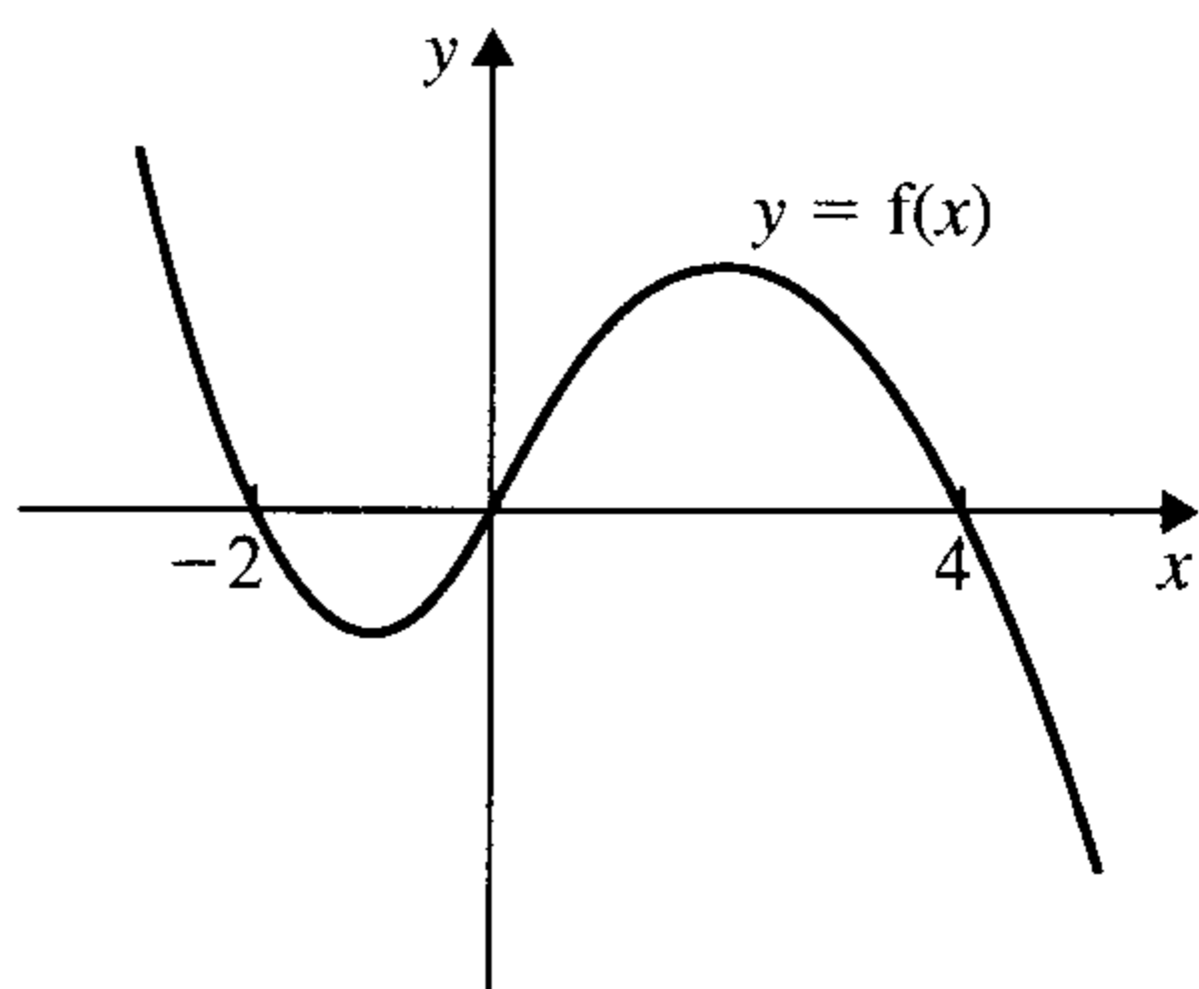
12 The function  $f$  is defined by  $f(x) = x^2 - 4x - 5, x \in \mathbb{R}, x \geq 2$ .

- a Find the range of  $f$ .
- b Write down the domain and range of  $f^{-1}$ .
- c Sketch the graph of  $f^{-1}$ , showing any points where the graph intersects the coordinate axes.

13 Sketch the graphs of the following, marking where the graphs cross the axes.

- a  $y = |x - 3|$
- b  $y = |3x + 1|$
- c  $y = |x^2 - 1|$
- d  $y = |\sin x|$  for  $0 \leq x \leq 2\pi$ .

14 The graphs of  $y = f(x)$  and  $y = g(x)$  are shown.



Sketch the graphs of

- a  $y = |f(x)|$
- b  $y = |g(x)|$
- c  $y = f(|x|)$
- d  $y = g(|x|)$ .

15 Solve the inequalities.

- a  $|x - 1| < |x + 2|$
- b  $|2x + 1| > |x - 1|$

16 Solve the inequalities.

- a  $|x - 1| < 5$
- b  $|2x - 3| > 1$

17 a Sketch the graph of  $y = |x^2 - 4|$ .

b Solve the inequality  $|x^2 - 4| > 5$ .

18 a On the same axes, sketch the graphs of  $y = |2x + 1|$  and  $y = \frac{2}{x}$ .

b How many solutions are there to the equation  $|2x + 1| = \frac{2}{x}$ ?